



## Ash Croft Primary Academy

### Calculation & Fluency Policy – Progression in Multiplication

Last updated: 10th February 2022



This document outlines the progression in multiplication strategies throughout our academies. Teaching staff should consider using previously taught written methods as part of visually representing mental methods later in a child's school journey. For example, using the 'sorting into groups' method (taught as a written method in much of KS1) as a way to visually represent mental methods in Key Stage 2.

It has been carefully put together in line with the National Curriculum (2014), the Government's non-statutory guidance for teaching mathematics (June 2020) and our existing approach to teaching mathematics. This document has been organised respective of age-related expectations and learning should still be differentiated appropriately.

#### Progression in learnt multiplication facts

Written multiplication strategies are learnt formally in Key Stage 2, with 'long multiplication' being taught in Year 6. The Multiplication Tables Check (MTC) in Year 4 aims to ensure children are meeting the National Curriculum objective *"to recall multiplication and division facts for multiplication tables up to  $12 \times 12$ "*. Learning times tables by heart is fundamentally important to ensure children can access the full curriculum beyond Year 4. With this in mind, the diagram below shows our age-related expectations for learning times tables.

By the end of Year 2			By the end of Year 3			By the end of Year 4				
10x	5x	2x	4x	8x	3x	6x	9x	7x	11x	12x

# Year 1

**In Year 1**, pupils should learn how to count in multiples of 2, 5 and 10 so that they are ready to progress to multiplication involving groups of 2, 5 and 10 in Year 2. As with counting in ones within 100, this is a key skill that will need to be practised throughout Year 1.

By the end of Year 1, pupils should be fluent in counting in these multiples, and our approach is to introduce the multiplication and division symbols ( $\times$  and  $\div$ ) as a way of presenting written calculations during Year 1.

Children should be taught at this stage that the first number of a multiplication calculation is how many groups there are, and the second number is the number of items in each group. The final number is how many items there are altogether.

Number of groups	Number in each group	Total number of items
↓	↓	↓
4	$\times$ 5	= 20
Multiplier	Multiplicand	Product

Picture examples

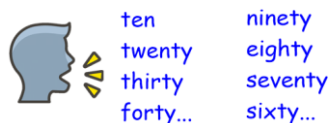
Lesson videos

## Counting

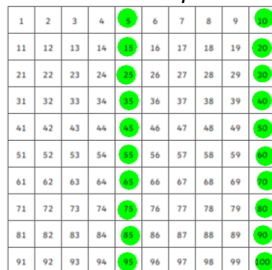
To confidently count in multiples of 2, 5 and 10, forwards and backwards counting practice should include:

- reciting just the number names (for example, "ten, twenty, thirty..."), without the support of visual representations

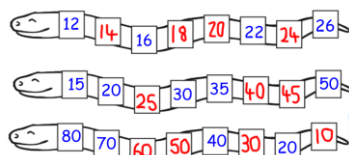
Counting forwards and backwards in 2s, 5s and 10s



- counting with the support of visual representations and gestural patterns. For example, pupils could point to numerals on a number line or a 100 square.

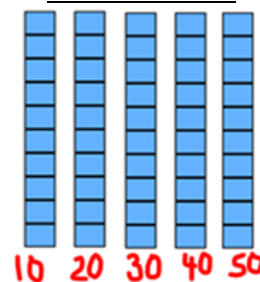


- starting the forwards counting sequence with numbers other than 2, 5 or 10

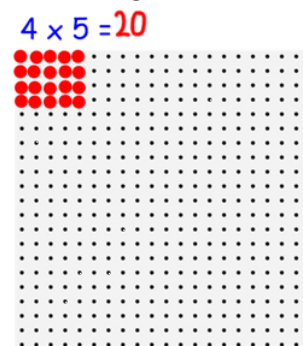


## Practical approaches

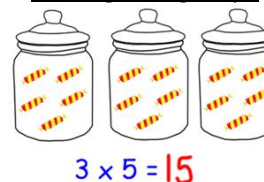
### Base Ten Blocks



### Peg boards



### Sorting into groups

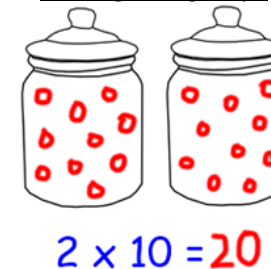


## Pictorial approaches

### Using pictorial approaches



### Sorting into groups



## Year 2

**In Year 2**, pupils should recognise repeated addition contexts, representing them with multiplication equations and calculating the product, within the 2, 5 and 10 multiplication tables.

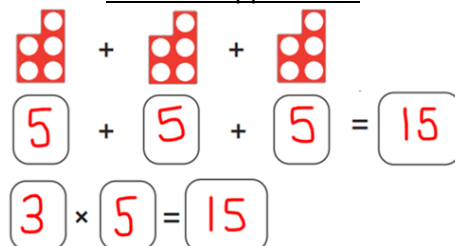
Pupils who are sufficiently fluent in Year 2 multiplicative calculations are not reliant on drawing arrays or using number lines as tools to calculate. Pupils should have sufficient conceptual understanding to recognise these as models of multiplication and division. Skip counting should be common practice to help pupils learn the 10, 5 and 2x tables by heart.

Pupils need to be able to represent 4 fives (or 5, 4 times) as both  $4 \times 5$  and  $5 \times 4$ . They should be able to use commutativity to solve, for example, 2 sevens, using their knowledge of 7 twos. This is something that is likely to not have been introduced in Year 1 and so should be key learning.

Picture examples

### Repeated addition

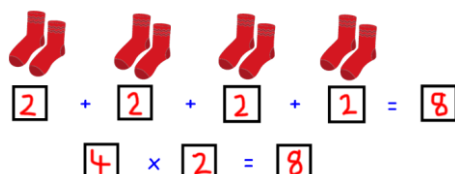
#### Concrete approaches



$$5 + 5 + 5 = 15$$

$$3 \times 5 = 15$$

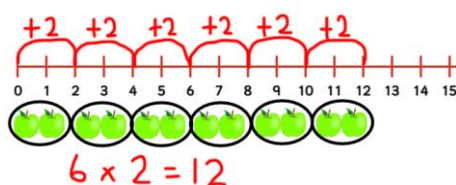
#### Pictorial approaches



$$2 + 2 + 2 + 2 = 8$$

$$4 \times 2 = 8$$

#### Showing groups on a number line

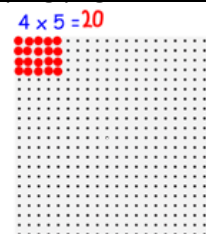


Lesson videos



### Arrays

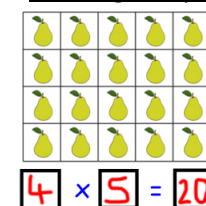
#### Practical (recapping peg boards from Y1)



#### Drawing arrays

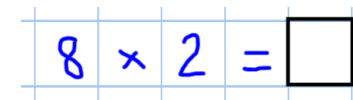


#### Reading arrays



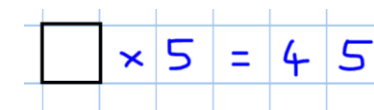
### More formal contexts

#### Identifying products



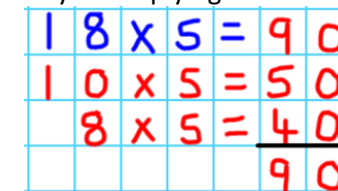
$$8 \times 2 = \square$$

#### Solving missing-factor problems



$$\square \times 5 = 45$$

#### Semi-formal method (always multiplying the tens first)



$$18 \times 5 = 90$$






$$10 \times 5 = 50$$

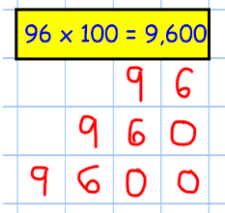
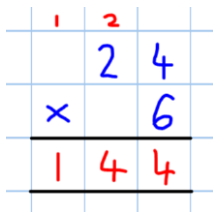






$$8 \times 5 = 40$$

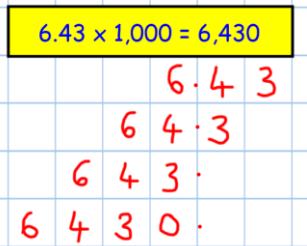

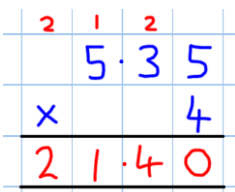

$$90$$



Year 3	<p><b>In Year 3</b>, pupils should be able to recall multiplication facts, and corresponding division facts, for times tables learned in Year 2 (10, 5 and 2 x tables). They should then progress to learning the 3, 4 and 8 x tables during Year 3. Pupils will recognise products in these multiplication tables as multiples of the corresponding number.</p>	Picture examples	<p><u>Identifying products</u></p> 	<p><u>Solving missing-factor problems</u></p> 	<p><u>Grid method</u></p> <p><math>23 \times 4 = 92</math></p> <table border="1"><tr><td>x</td><td>20</td><td>3</td></tr><tr><td>4</td><td>80</td><td>12</td></tr></table> 	x	20	3	4	80	12
	x	20	3								
4	80	12									
<p><i>Pupils should also be fluent in interpreting contextual multiplication and division problems, identifying the appropriate calculation and solving it using automatic recall of the relevant fact. As pupils become fluent with multiplication facts, they should develop fluency in related calculations by scaling facts by 10. For example, if <math>3 \times 4 = 12</math>, then <math>30 \times 4 = 120</math>. And, if <math>12 \div 3 = 4</math>, then <math>120 \div 4 = 30</math>.</i></p>	Lesson videos										

Year 4	<p><b>In Year 4</b>, the main multiplication calculation focus should be the ability to recall all multiplication table facts. Pupils who leave Year 4 fluent in these facts have the best chance of mastering short multiplication in Year 5. As they become fluent with times tables, pupils should begin to scale by powers of 10 using their knowledge of place value.</p>	Picture examples	<p><u>Identifying products</u></p> <p><math>8 \times 9 = \square</math></p> <p><math>\square = 3 \times 12</math></p> <p><math>6 \times 6 = \square</math></p>	<p><u>Solving missing-factor and divisor problems</u></p> <p><math>8 \times \square = 48</math></p> <p><math>121 = \square \times 11</math></p> <p><math>35 \div \square = 7</math></p> <p><math>6 = 36 \div \square</math></p>	<p><u>Using the inverse to solve missing dividend problems</u></p> <p><math>\square \div 4 = 7</math></p> <p><math>6 = \square \div 5</math></p> <p><math>9 = \square \div 9</math></p>	<p><u>Multiplying by 10, 100 and 1000</u></p> <p><math>18 \times 100 = 1,800</math></p> <p><math>\begin{array}{r} 18 \\ 180 \\ 1800 \end{array}</math></p>	<p><u>Grid method</u></p> <p><math>132 \times 6 = 792</math></p> <table><tr><td><math>\times</math></td><td>100</td><td>30</td><td>2</td></tr><tr><td>6</td><td>600</td><td>180</td><td>12</td></tr></table> <p><math>\begin{array}{r} 600 \\ 180 \\ + 12 \\ \hline 792 \end{array}</math></p>	$\times$	100	30	2	6	600	180	12
	$\times$		100	30	2										
6	600	180	12												
<p><i>Pupils should also be fluent in interpreting contextual multiplication and division problems, identifying the appropriate calculation and solving it using automatic recall of the relevant fact. As pupils become fluent with multiplication facts, they should develop fluency in related calculations by scaling facts by 100. For example, if <math>3 \times 4 = 12</math>, then <math>300 \times 4 = 1,200</math>. And, if <math>12 \div 3 = 4</math>, then <math>1,200 \div 4 = 300</math>.</i></p>															

Year 5	<p><b>In Year 5</b>, pupils should be able to multiply whole numbers with up to 4 digits by any 1-digit number using the short multiplication method. In addition, they should be able to multiply by powers of 10 using their knowledge of place value.</p> <p><i>Pupils should be fluent in interpreting contextual problems to decide when multiplication is the appropriate operation to use, including as part of multi-step problems. Pupils should use short multiplication as appropriate to solve these calculations.</i></p>	Picture examples	<p><u>Multiplying by 10, 100 and 1000</u></p> 	<p><u>Short multiplication (2x1)</u></p> 	<p><u>Short multiplication (3x1)</u></p> 	<p><u>Short multiplication (4x1)</u></p> 
		Lesson videos				

Year 6	<p><b>In Year 6</b>, pupils should continue to practise multiplying a 4-digit whole number by any 1-digit number using short multiplication. Pupils should now also use this method to multiply decimals by 1-digit numbers as well as using long multiplication to multiply a 2-digit number by a 2 or 3-digit number. In addition, they should be able to multiply by powers of 10 using their knowledge of place value.</p> <p><i>Pupils should be fluent in interpreting contextual problems to decide when multiplication is the appropriate operation to use, including as part of multi-step problems. Pupils should use short or long multiplication as appropriate to solve these calculations.</i></p> <p><i>Pupils should also learn to check their short and long multiplication calculations with a calculator so that they know how to use one. This will help pupils when they progress to Key Stage 3.</i></p>	Picture examples	<p><u>Multiplying by 10, 100 and 1000</u></p> 	<p><u>Short multiplication</u></p> 	<p><u>Short multiplication with decimal numbers</u></p> 	<p><u>Long multiplication (2x2 and 3x2)</u></p> 
		Lesson videos	